

## A Comparison of Expectations in OAC Finite Mathematics and Grade 12 Mathematics of Data Management

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*Items related to expected use of technology (handheld as well as computer software) appear in bold italics.*

Content Area	OAC Finite Mathematics	Grade 12 Mathematics of Data Management
Matrices	1. Applications of Matrix Algebra <ul style="list-style-type: none"> <li>a) using vector and matrices to represent information</li> <li>b) relating addition of matrices and multiplication by a scalar to applications                             <ul style="list-style-type: none"> <li>• inventory</li> <li>• production</li> </ul> </li> <li>c) relating multiplication of matrices to applications                             <ul style="list-style-type: none"> <li>• production costs</li> <li>• coding</li> <li>• transportation networks</li> <li>• simple Markov processes</li> </ul> </li> </ul>	Very similar expectations.  Include applications of row and column sums.  Greater emphasis on application to problems.  <i>Expectation that students will demonstrate proficiency with and without aid of technology.</i>  <b>NO MARKOV PROCESSES.</b>  Application to the work on graph theory in the Organization of Data for Analysis strand.
	2. Solving Systems of Equations and Inequalities <ul style="list-style-type: none"> <li>a) linear functions, piecewise linear functions and step functions to model situations</li> <li>b) solving problems with up to 4 linear equations by elimination</li> <li>c) augmented matrices</li> <li>d) row-reduced echelon form</li> <li>e) using technology to solve systems</li> <li>f) using constraints to generate inequalities</li> <li>g) graphical solution of systems of inequalities</li> <li>h) geometric linear programming</li> <li>i) solving problems using linear programming and simplex (optional)</li> </ul>	NOT IN THE COURSE. (Some of this content now part of the new Geometry and Discrete Mathematics course, MGA4U)

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Combinatorics	1. Permutations a) r-arrangements of n different things b) factorial c) arrangements when some are alike	Less emphasis on solution of algebraic equations and simplification of complicated expressions. The more difficult types of permutation counting problems are part of the new Geometry and Discrete Mathematics course, MGA4U
	2. Combinations a) r-subsets of a set of n objects b) number of subsets c) $C(n, r)$ , $\binom{n}{r}$ notation and formula d) indirect reasoning	Less emphasis on solution of algebraic equations and simplification of complicated expressions. The more difficult types of combination counting problems are part of the new Geometry and Discrete Mathematics course, MGA4U  Use Venn diagrams as a tool for organizing information in counting problems.
	3. The Binomial Theorem a) Relating Pascal's triangle to the expansion of a binomial. $\binom{n}{r} + \binom{n}{r+1} = \binom{n+1}{r+1}$ b) Proving the Binomial Theorem using number of r-subsets. c) Mathematical Induction (optional) d) Using the general term in the expansion to determine coefficients of a given power.	Identify patterns in Pascal's triangle and relate the terms of Pascal's triangle to values of $\binom{n}{r}$ to the expansion of a binomial $(a + b)^n$ , and to the solution of related problems.  <b>NO EXPECTATION REGARDING PROOF OF THE BINOMIAL THEOREM.</b>
	4. Finite Series a) – c) Proving and using formulas for arithmetic, geometric and infinite geometric series and sum of binomial coefficients d) telescoping sums (optional) e) other sums (optional)	NOT IN THE COURSE.

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Probability and Applications	1. Probability <ul style="list-style-type: none"> <li>a) Relating concepts of probability to applications.</li> <li>b) Investigating situations that may be represented by uniform probability models.</li> <li>c) Probability of an event.                             <ul style="list-style-type: none"> <li>• ratio of favourable outcomes to total equally likely outcomes</li> <li>• use counting methods to determine probabilities</li> </ul> </li> <li>d) Investigate rules for probability calculations and their uses.                             <ul style="list-style-type: none"> <li>• <math>P(A \text{ or } B)</math> (mutually exclusive and otherwise)</li> <li>• <math>P(A \text{ and } B)</math> (independent and otherwise)</li> <li>• <math>P(A   B)</math> and <math>P(A')</math></li> </ul> </li> <li>e) Tree diagrams.</li> </ul>	General flavour is pretty much the same.  <b>SPECIFIC EXPECTATIONS RELATED TO SIMULATIONS:</b> <ul style="list-style-type: none"> <li>• Identify the advantages of using simulations in contexts.</li> <li>• <i>Design and carry out simulations</i> to estimate probabilities in situations for which the calculation of the theoretical probabilities is difficult or impossible.</li> <li>• Assess the validity of some simulation results by comparing them with the theoretical probabilities, using the probability concepts developed in the course.</li> </ul> <p><b>This implies the use of technology as well as hands-on simulations.</b></p>
	2. Applications of Probability <ul style="list-style-type: none"> <li>a) Random Variables.</li> <li>b - c) Recognizing and calculating probabilities for situations using uniform distributions</li> <li>d - e) Recognizing and calculating probabilities for situations using binomial distributions</li> <li>f - g) Recognizing and calculating probabilities for situations using hypergeometric distributions</li> </ul>	<ul style="list-style-type: none"> <li>• identify examples of discrete random variables</li> <li>• construct a discrete probability distribution function by calculating the probabilities of a discrete random variable;</li> <li>• calculate expected values and interpret them within applications as averages over a large number of trials;</li> <li>• determine probabilities, using the binomial distribution</li> </ul>

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Statistics	<p>CONSIDERED A SUB-HEAD UNDER PROBABILITY.</p> <p>3. Statistics</p> <p>a) Frequency diagrams</p> <ul style="list-style-type: none"> <li>• frequency (histograms)</li> <li>• relative frequency</li> <li>• cumulative frequency</li> </ul> <p>b) Summary statistics (1-variable)</p> <ul style="list-style-type: none"> <li>• percentile</li> <li>• range</li> <li>• deviation</li> <li>• mean deviation</li> <li>• standard deviation</li> </ul> <p>c) Investigating situations modelled by a normal distribution</p> <ul style="list-style-type: none"> <li>• percentages within 1 or 2 s.d. of the mean</li> </ul> <p>d) Using normal distribution to approximate the binomial distribution</p>	<p><b>MUCH MORE EMPHASIS ON THE USE OF TECHNOLOGY TO DETERMINE STATISTICS.</b></p> <p>MORE EMPHASIS ON INTERPRETING STATISTICS TO DESCRIBE CHARACTERISTICS OF A DATA SET</p> <p>Collecting Data</p> <ul style="list-style-type: none"> <li>• understand purpose and use of various sampling techniques                             <ul style="list-style-type: none"> <li>• simple random</li> <li>• systematic</li> <li>• stratified random</li> </ul> </li> <li>• bias and variability                             <ul style="list-style-type: none"> <li>• describe types of bias in surveys</li> <li>• illustrate sampling bias and variability by repeated sampling of a known population</li> </ul> </li> <li>• organize and summarize data from secondary sources using technology</li> </ul> <p>One Variable Statistics</p> <ul style="list-style-type: none"> <li>• understand use of, interpret and <i>compute using technology</i> <ul style="list-style-type: none"> <li>• mean, median, mode</li> <li>• range, interquartile range</li> <li>• variation, standard deviation</li> <li>• z-scores, percentiles</li> </ul> </li> </ul>

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Statistics		<p>Normal Distribution</p> <ul style="list-style-type: none"> <li>• Identify common distributions.                             <ul style="list-style-type: none"> <li>• bimodal, U-shaped, exponential</li> <li>• skewed, normal</li> </ul> </li> <li>• Use properties of the Normal Distribution to solve problems.                             <ul style="list-style-type: none"> <li>• location of mean, median and mode</li> <li>• symmetry about mean</li> <li>• 1 and 2 standard deviation spreads</li> <li>• make probability statements about normal distributions in applications</li> </ul> </li> </ul> <p>Two Variable Statistics</p> <ul style="list-style-type: none"> <li>• linear regression and correlation coefficient                             <ul style="list-style-type: none"> <li>• measure of fit of a linear model to a scatter graph</li> <li>• <i>calculate using technology</i></li> </ul> </li> <li>• understand the distinction between mathematical correlation and cause-and-effect                             <ul style="list-style-type: none"> <li>• describe possible misuses</li> </ul> </li> </ul> <p>Evaluating Validity</p> <ul style="list-style-type: none"> <li>• explain examples of use/misuse of statistics in the media</li> <li>• assess validity of conclusions by analyzing sources of bias or <i>recomputing statistics</i></li> <li>• explain use of indices</li> </ul>

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Organization of Data for Analysis	NOT IN THE COURSE.	<p><b>MAJOR EMPHASIS ON LOCATING AND ORGANIZING DATA FOR ANALYSIS USING TECHNOLOGY (see project strand).</b></p> <p>Organizing Data</p> <ul style="list-style-type: none"> <li>• locate data                             <ul style="list-style-type: none"> <li>• <i>search databases</i></li> <li>• <i>use Internet</i> as a source for databases</li> <li>• <i>create databases using spreadsheet or database software</i></li> </ul> </li> </ul> <p>Using Diagrams to Solve Problems</p> <ul style="list-style-type: none"> <li>• represent processes                             <ul style="list-style-type: none"> <li>• simple iterative processes</li> <li>• branches and loops (flow diagrams)</li> </ul> </li> <li>• represent complex tasks, issues                             <ul style="list-style-type: none"> <li>• tree diagrams</li> <li>• network diagrams</li> <li>• cause-and-effect diagrams</li> <li>• time lines</li> </ul> </li> <li>• solve network problems using introductory graph theory (see matrices)</li> </ul> <p><b>SUGGEST THIS IS BACKGROUND FOR THE FINAL PROJECT.</b></p>

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Content Area	OAC Finite Mathematics	Grade 12 Mathematics of Data Management
Integration of the Techniques of Data Management	NOT IN THE COURSE	<p>By the end of this course, students will:</p> <ul style="list-style-type: none"> <li>• carry out a culminating project on a <i>topic or issue of significance that requires the integration and application of the expectations of the course</i>;</li> <li>• <i>present a project</i> to an audience and critique the projects of others.</li> </ul> <p>Carrying Out a Culminating Project</p> <ul style="list-style-type: none"> <li>• pose a <i>significant problem</i> whose solution would require the organization and analysis of a <i>large amount of data</i>;</li> <li>• <i>select and apply the tools of the course</i> (e.g., methods for organizing data, methods for calculating and interpreting measures of probability and statistics, methods for data collection) to design and carry out a study of the problem;</li> <li>• compile a clear, well-organized, and fully justified <i>report of the investigation and its findings</i>.</li> </ul> <p>Presenting and Critiquing Projects</p> <ul style="list-style-type: none"> <li>• create a summary of a project to present within a restricted length of time, <i>using communications technology</i> effectively;</li> <li>• answer questions about a project, fully justifying mathematical reasoning;</li> <li>• critique the mathematical work of others in a constructive fashion.</li> </ul> <p><b>THE PROJECT SHOULD MAKE UP A SIGNIFICANT COMPONENT OF A STUDENT’S FINAL GRADE IN THE COURSE.</b></p> <p><b>THE PROJECT WILL REPRESENT A SUBSTANTIAL INVESTMENT OF TIME AND EFFORT AND WILL REQUIRE TECHNOLOGY.</b></p> <p><b>THE PROJECT PROCESS WILL HAVE TO BE MONITORED CAREFULLY</b></p>